



2. GA-based TSP TSP is known as an NP-hard program that causes a computational explosion. For instance, finding the shortest route through 36 cities needs to examine  $36!$  ( $= 36 \times 35 \times \dots \times 1$ ) combinations. GA is quite effective to reduce TSP's computation time while reaching a semi-optimal trip (but not the shortest path). Consider a travel through 36 cities, each named with one of the 36 characters such as A~Z and 0~9.

ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789 is one possible trip. In GA, this string and each city in it can be considered as a chromosome and a gene respectively. We will first generate 50,000 different trips or chromosomes, and then repeat 150 iterations or so-called generations, each including: (1) `evaluate()`: evaluates the distance of each trip and sorts out all the trips in the shortest-first order. Memorize the current shortest trip as a tentative answer if it is shorter than the previous. (2) `select()`: selects the shortest 25,000 trips as parents. (3) `crossover()`: generates 25,000 off-springs from the parents. More specifically, we spawn a pair of `child[i]` and `child[i+1]` from `parent[i]` and `parent[i+1]`. (4) `mutate()`: randomly chooses two distinct cities (or genes) in each trip (or chromosome) with a given probability, and swaps them. (5) `populate()`: populate the next generation by replace the bottom 25,000 trips with the newly generated 25,000 off-springs.

3. Crossover Algorithm The key to GA-based TSP is to design a suitable crossover algorithm. A typical crossover generates `child[i]` by combining the first half of `parent[i]`'s genes and the last half of `parent[i+1]`'s genes, whereas gives `child[i+1]` the last half of `parent[i]`'s genes and the first half of `parent[i+1]`'s genes. However, this crossover does not work in TSP. For example in a TSP program for visiting only eight cities, consider two parents: `parent[i] = ABCDEFGH` `parent[i+1] = HGABFECD` Their children will be: `child[i] = ABCDFECD`  
`child[i+1] = HGABEFGH`

`Child[i]` and `child[i+1]` will end up with revisiting CD and GH respectively. To address this problem, we will use a greedy crossover algorithm: We select the first city of `parent[i]`, compares the cities leaving that city in `parent[i]` and `parent[i+1]`, and chooses the closer one to extend `child[i]`'s trip. If one city has already appeared in the trip, we choose the other city. If both cities have already appeared, we randomly select a non-selected city. Thereafter, we generate `child[i+1]`'s trip as a complement of `child[i]`.